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Aerodynamic Analysis of a Scramjet Inlet and Isolator

Inês Micaela da Costa Cardoso

Supervisor:

Prof. Mário António Prazeres Lino da Silva

Examination Committee:

Chairperson: Prof. Filipe Szolnoky Ramos Pinto Cunha

Supervisor: Prof. Mário António Prazeres Lino da Silva

Member of the Committee: Prof. José Carlos Fernandes Pereira

January 2021

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Fig 1. Scramjet Concept Art [1].

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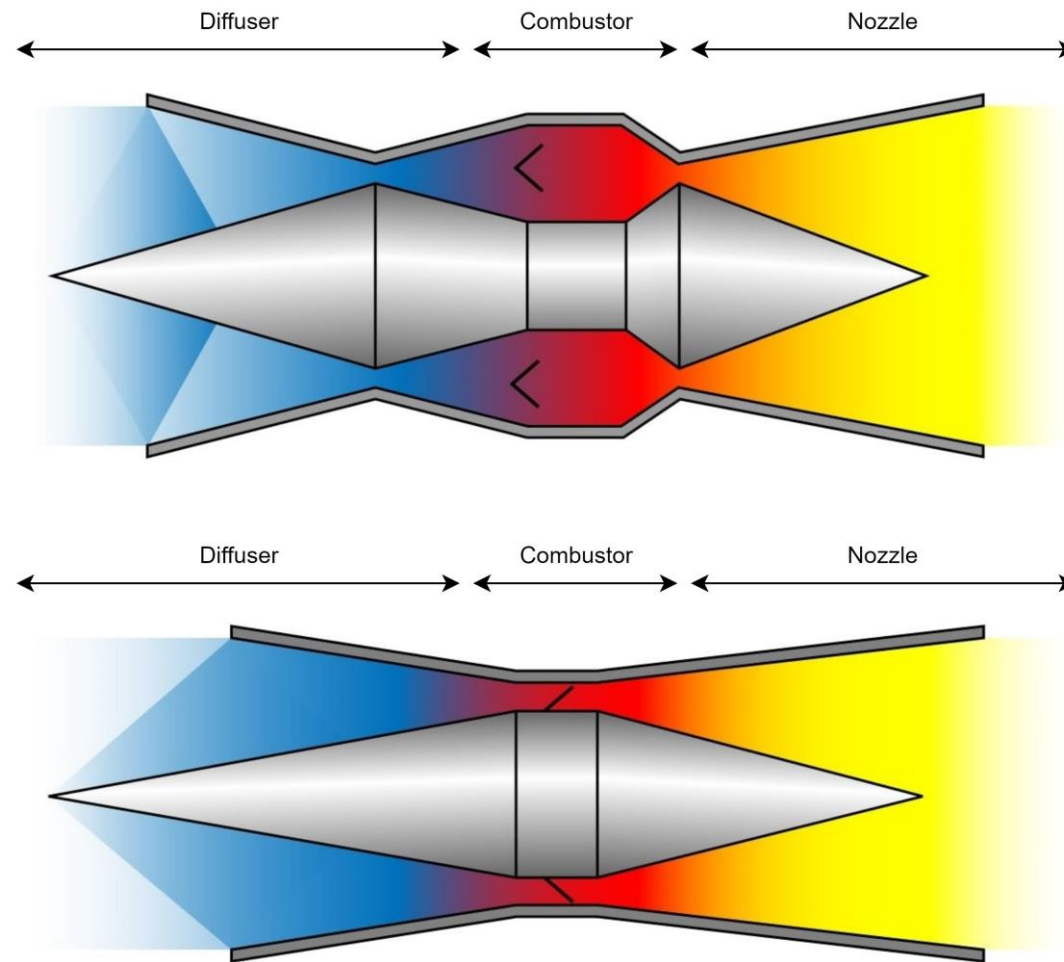


Fig. 2: Ramjet (top) and Scramjet (bottom) schematics. Adapted from [2].

Ramjet

Diffuser

Air is compressed to **subsonic** speeds by means of a shock wave system.



Combustor

Fuel is mixed with the compressed air and **subsonic** combustion takes place.



Nozzle

The high temperature exhaust is accelerated.



Thrust is generated.

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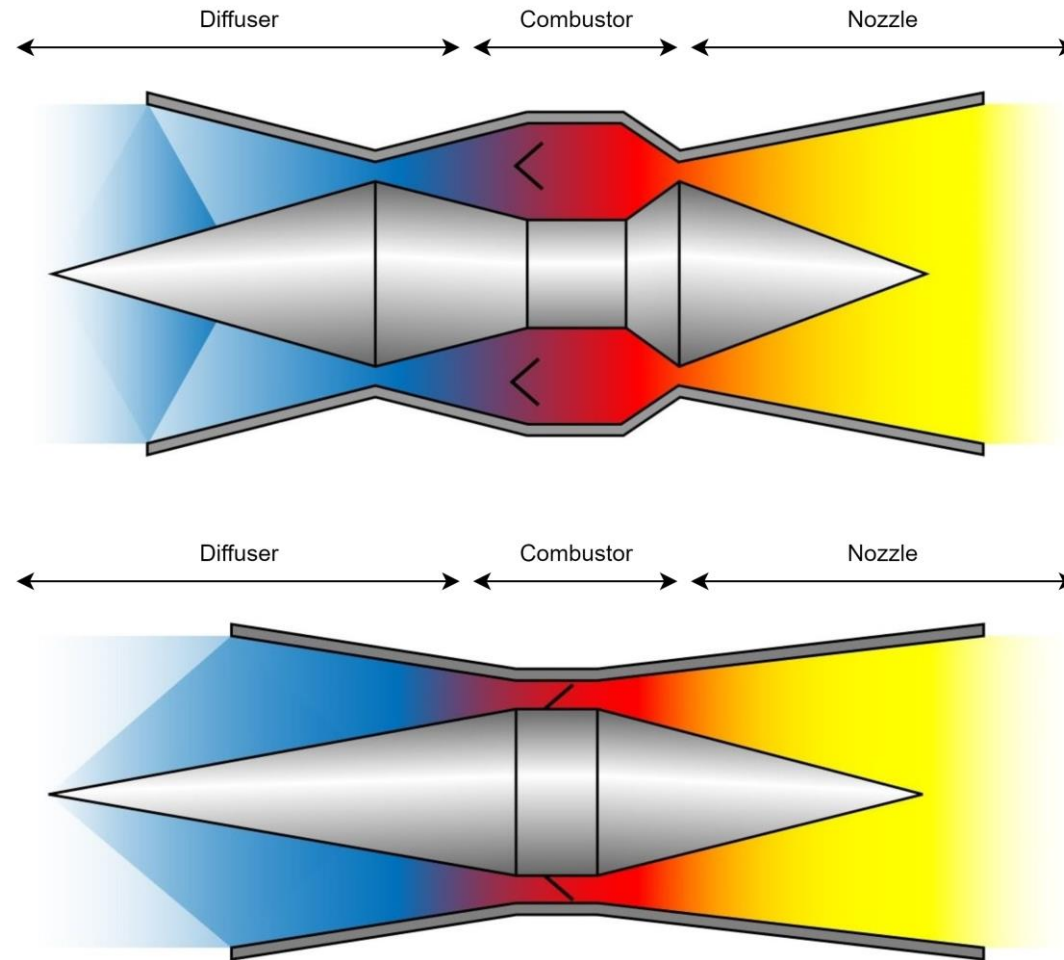


Fig. 2: Ramjet (top) and Scramjet (bottom) schematics. Adapted from [2].

Scramjet

Diffuser

Air is compressed to **supersonic** speeds by means of a shock wave system.



Combustor

Fuel is mixed with the compressed air and **supersonic** combustion takes place.



Nozzle

The high temperature exhaust is accelerated.



Thrust is generated.

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Operating Conditions

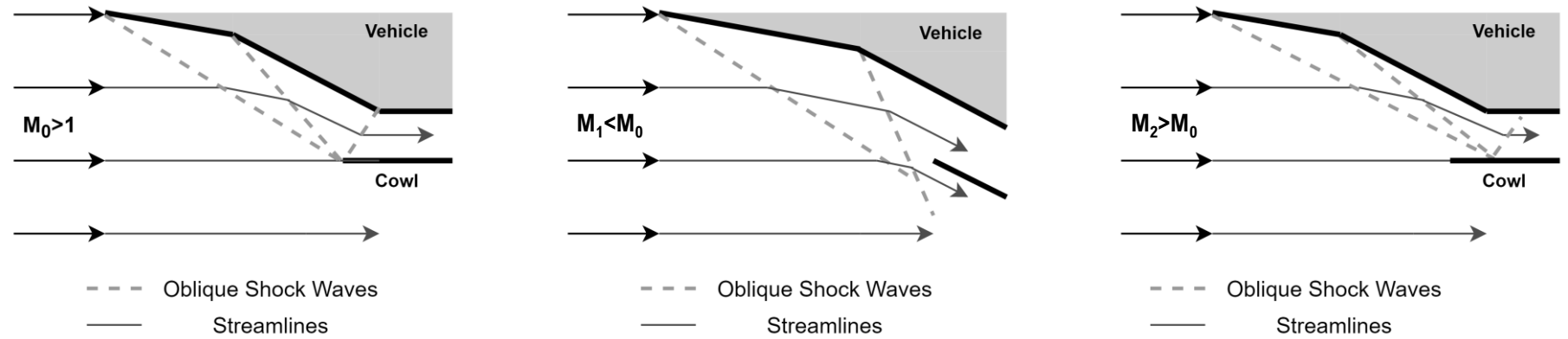


Fig. 3: Shock-on-lip condition (left), flow spillage (centre) and flow instability (right). Adapted from [3].

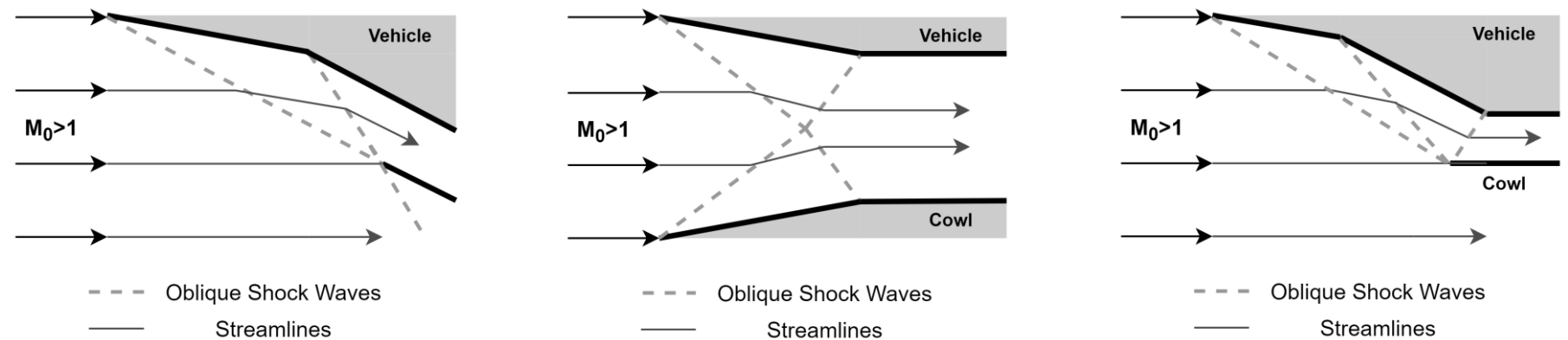


Fig. 4: External (left), internal (centre) and mixed (right) compression system layouts. Adapted from [3].

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Objectives

- Identification of a trajectory point of interest;
- Pre-analysis of a case study from the literature;
 - Validation of the SPARK code for solving scramjet compression system flows;
 - Identification of model shortfalls and their impact on the obtained flow.
- Assess the relative importance of non-equilibrium and high temperature effects;
- Compare the performance of the two-dimensional inlet present in the case study with that of an axisymmetric inlet with the same area and pressure ratios;
- Geometry parametric study;
 - Numerically assess the influence of several geometric parameters on the behaviour of the flow within the compression system.
- Study of an off-design trajectory point;
 - Numerically assess how performance is affected at an off-design trajectory point of Mach 7.

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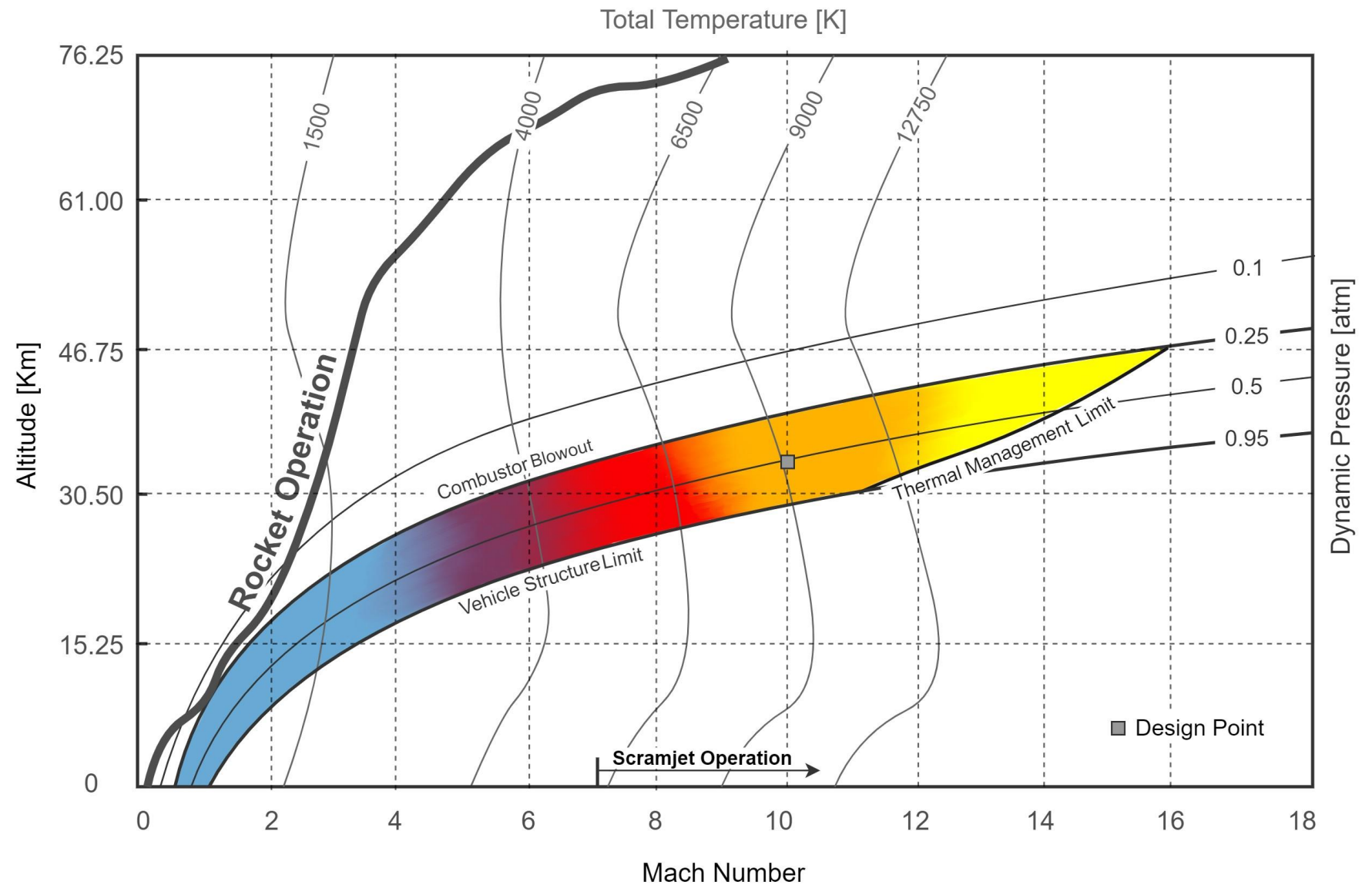


Fig. 5: Flight corridor as a function of Mach number and altitude. Identification of the selected trajectory point. Adapted from [4].

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Design Considerations

- The isolator should be long enough to prevent inlet unstart. The chosen reference presented an isolator length, **L = 0.5m**.
- The same reference suggests that, for a combustor entry velocity of 2400m/s and temperatures above 1000K, a back pressure of **50kPa** is expected to prevent inlet unstart and an acceptable combustor length.
- However supersonic combustion is expected to occur for isolator exit pressures as low as **20kPa [6]**.

θ_1 [°]	θ_2 [°]	H [m]	H/h
6.5	8.4	0.250	10

Table 1: Design Parameters for the baseline two-dimensional inlet [5].

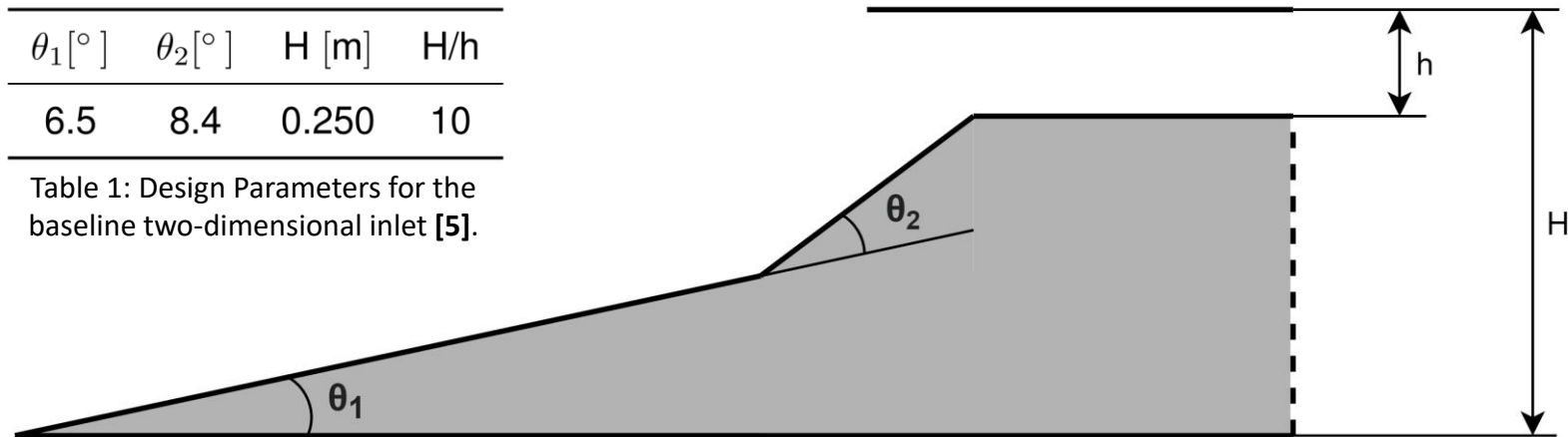


Fig. 6: Schematics of a mixed compression system. Design based on oblique shock theory.

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Non-Equilibrium Chemically Reacting Flow

- Navier-Stokes conservation equations apply, under the assumption of a continuum medium.
- The gas was considered to be a mixture of several chemical species to account for chemical reactions;
 - Considered species include: N_2 , N , O_2 , O , NO . No ionized species were considered.
- Thermal non-equilibrium is also expected to occur as a consequence of high temperature effects.
 - A two-temperature model, which considers the translational mode to be in equilibrium with the rotational mode, and the vibrational mode to be in equilibrium with the electronic mode was selected.

Oblique Shock Wave Theory

- Owing to its simplicity, oblique shock wave theory was used to dimension the different considered compression systems;
 - The Taylor Maccoll analysis was employed in the design of an axisymmetric compression system.

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Compression System Performance

- **Total pressure ratio** between isolator exit and freestream conditions;

$$\pi_c = \frac{p_{t_c}}{p_{t_\infty}} = \frac{p_c}{p_\infty} \left\{ \frac{1 + \frac{\gamma-1}{2} \text{Ma}_c^2}{1 + \frac{\gamma-1}{2} \text{Ma}_\infty^2} \right\}^{\frac{\gamma}{\gamma-1}}$$

- **Kinetic energy efficiency**, the ratio between the square of the velocity that the flow at the compression system exit would achieve if it were isentropically expanded to the freestream static pressure and the square of the freestream velocity;

$$\eta_{KE} = 1 - \frac{2}{(\gamma-1)\text{Ma}_\infty^2} \left\{ \frac{T_c}{T_\infty} \left(\frac{p_c}{p_\infty} \right)^{-\frac{\gamma-1}{\gamma}} - 1 \right\}$$

- **Compression efficiency**, the ratio of change in enthalpy that the flow at the combustor entry (or isolator exit) would incur if it were isentropically expanded to freestream static pressure, divided by the change in enthalpy that the flow is effectively put through.

$$\eta_c = \frac{(T_c/T_\infty) - (T_c/T_\infty)(p_c/p_\infty)^{-\frac{\gamma-1}{\gamma}}}{(T_c/T_\infty) - 1}$$

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The SPARK Code

- Is a computational CFD code for hypersonic flows, maintained at IPFN.
- Is capable of handling Euler and Navier-Stokes formulations.
- Allows for the choice of a perfect, frozen or chemically reacting gas.
- Allows for the inclusion of chemical kinetic and thermal non-equilibrium models.

Mesh and Boundary Conditions

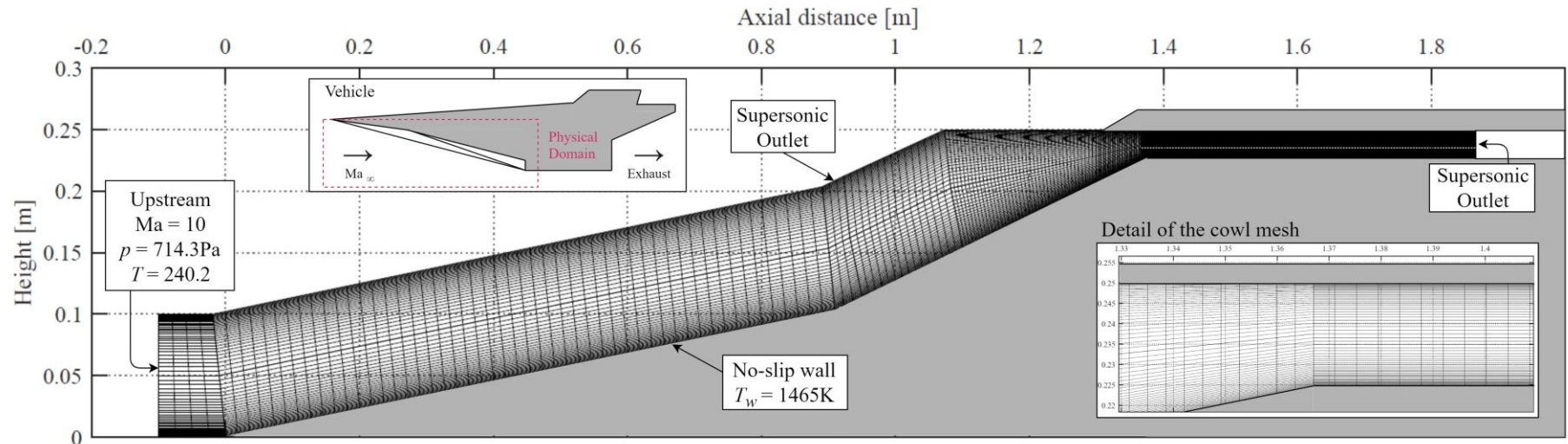


Fig. 7: Two-dimensional compression system mesh and boundary conditions. Not to scale.

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Mesh Convergence Study

Four different grid configurations were compared at two locations to allow for the choice of an appropriate mesh.

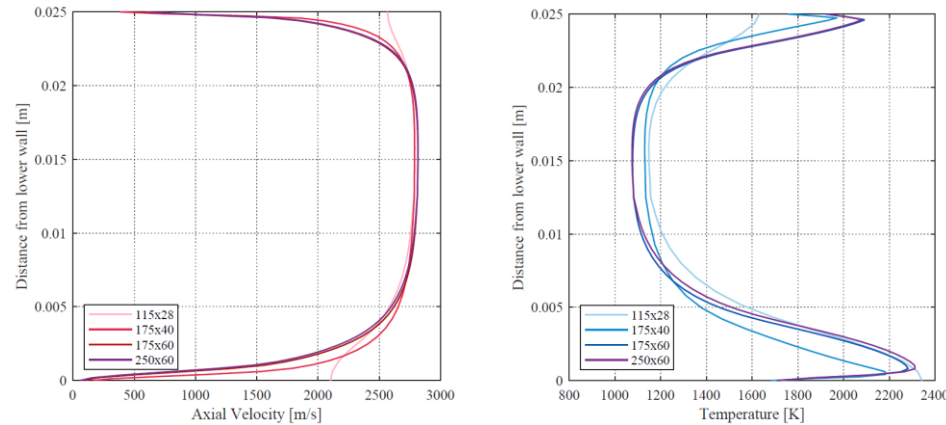


Fig. 8: Pressure and temperature profiles at $x=1.1\text{m}$, obtained for the mesh convergence study (2D).

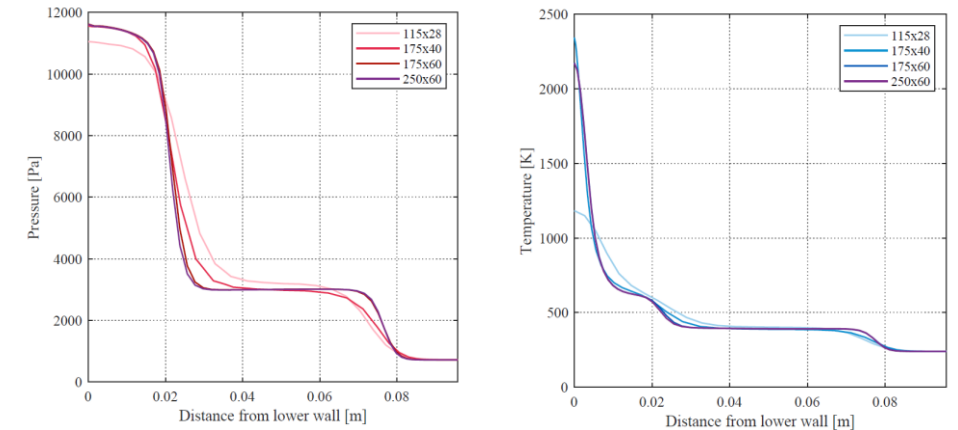


Fig. 9: Velocity and temperature profiles at the isolator exit, obtained for the mesh convergence study (2D).

The intermediate **175x60** grid was found to be the most suitable.

A similar mesh convergence study was conducted for the axisymmetric configuration and yielded an appropriate grid with **230x60** elements.

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Two-Dimensional Geometry: Frozen Flow

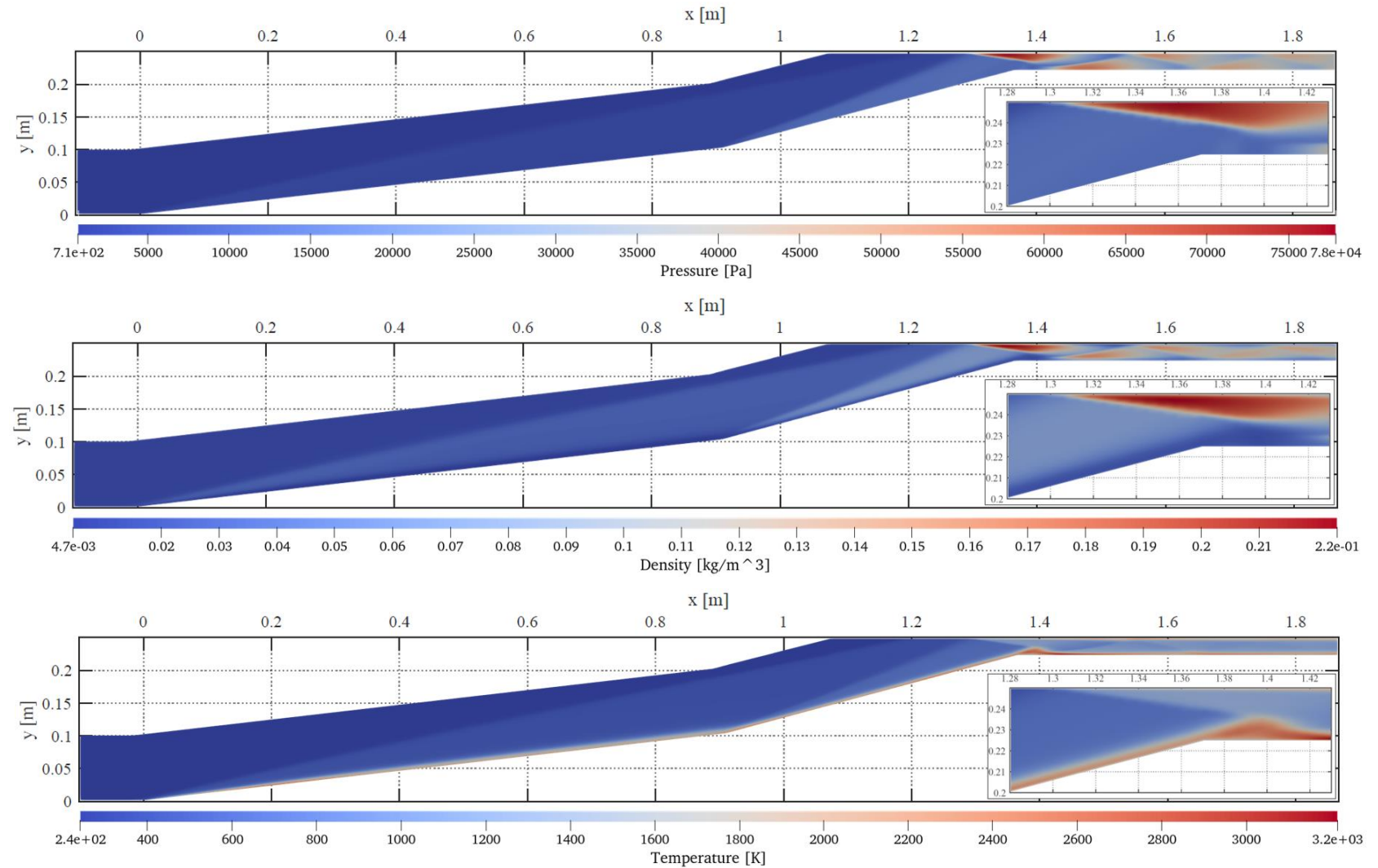


Fig. 10: Pressure, temperature and density fields obtained for the frozen-flow solution (2D).

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Two-Dimensional Geometry: Frozen Flow

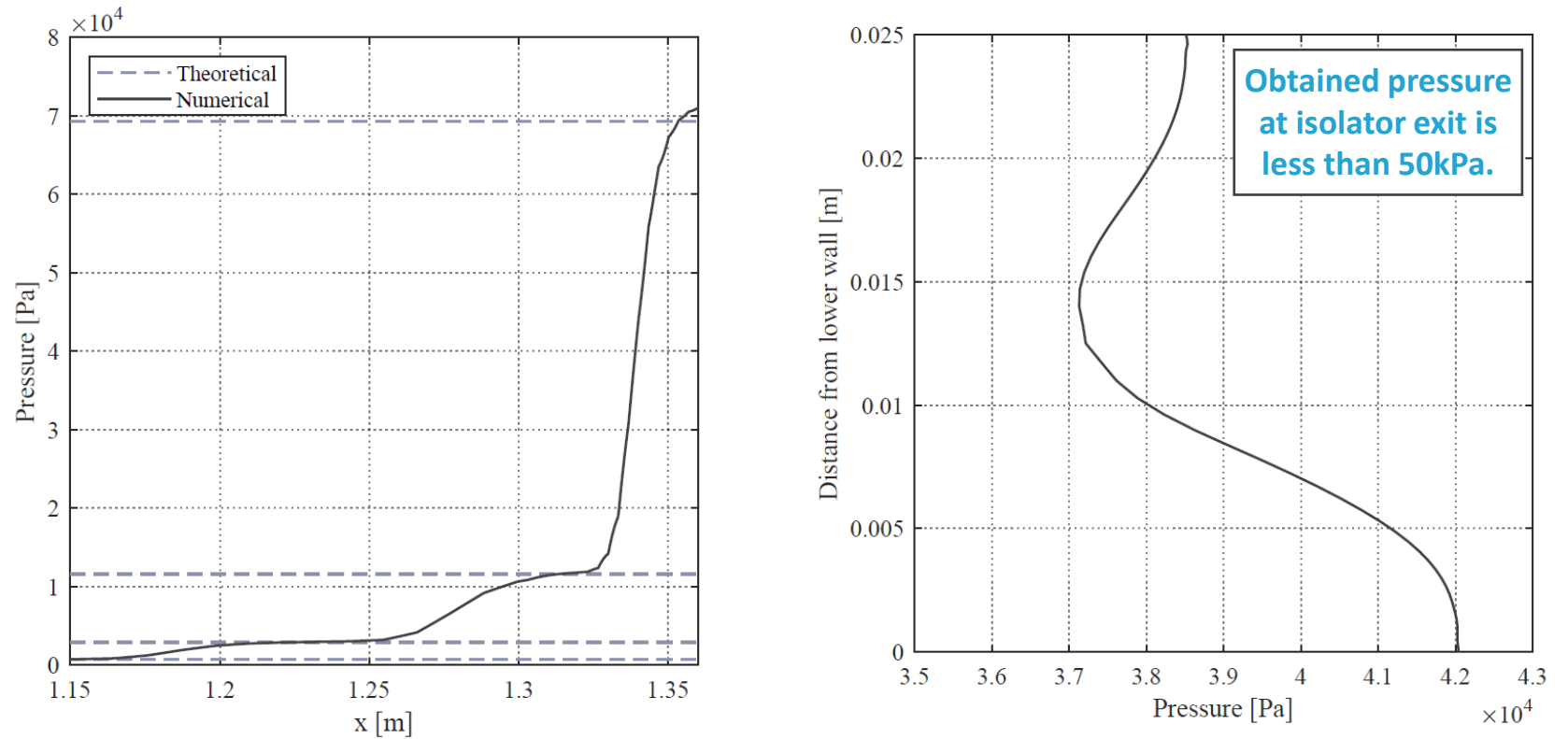


Fig. 11: Pressure variations across the first two oblique shock waves compared against oblique shock wave theory (left) and pressure profile at isolator exit (right).

Case	π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
Baseline	0.0793	0.9442	0.7898	0.7921

Table 2: Performance parameters for the baseline frozen flow solution.

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Two-Dimensional Geometry: Impact of Wall Temperature

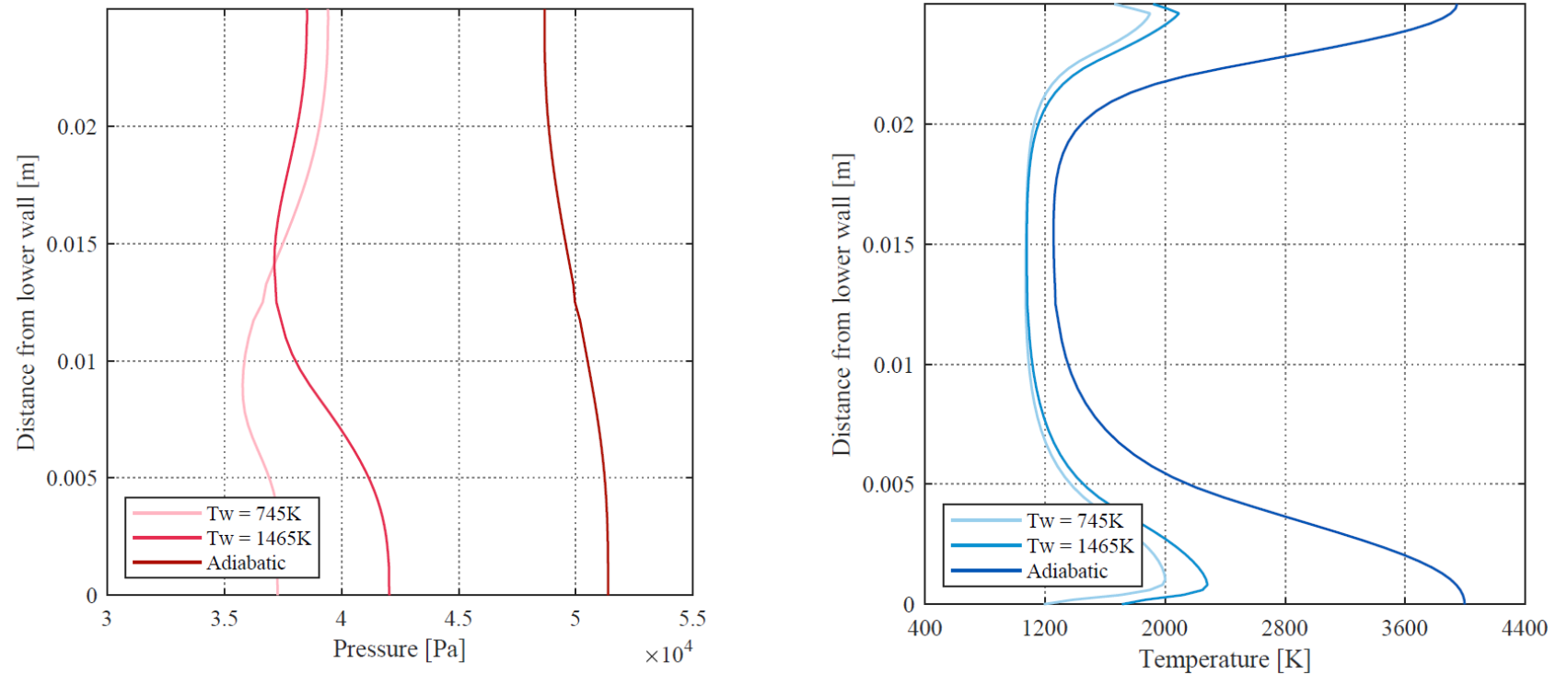


Fig. 12: Pressure and temperature profiles at the isolator exit for different wall boundary conditions.

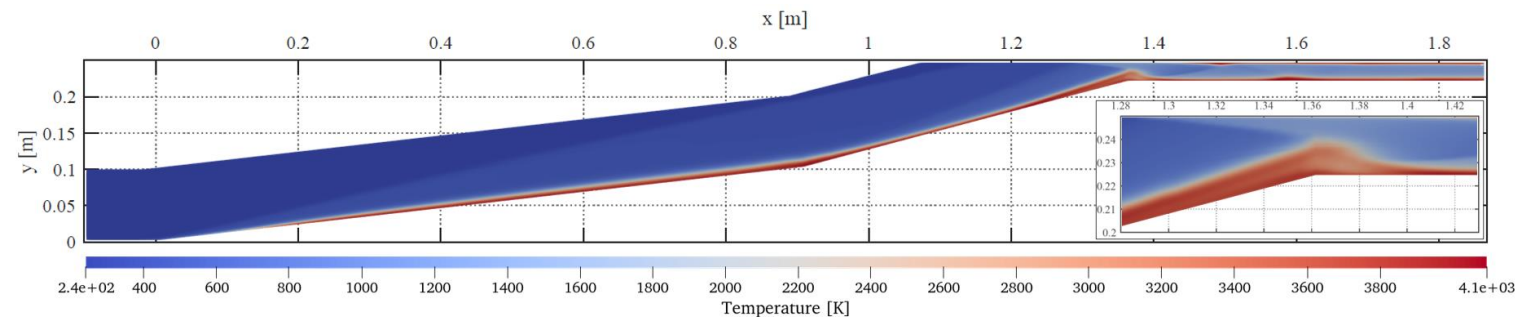


Fig. 13: Temperature field obtained for the adiabatic wall condition.

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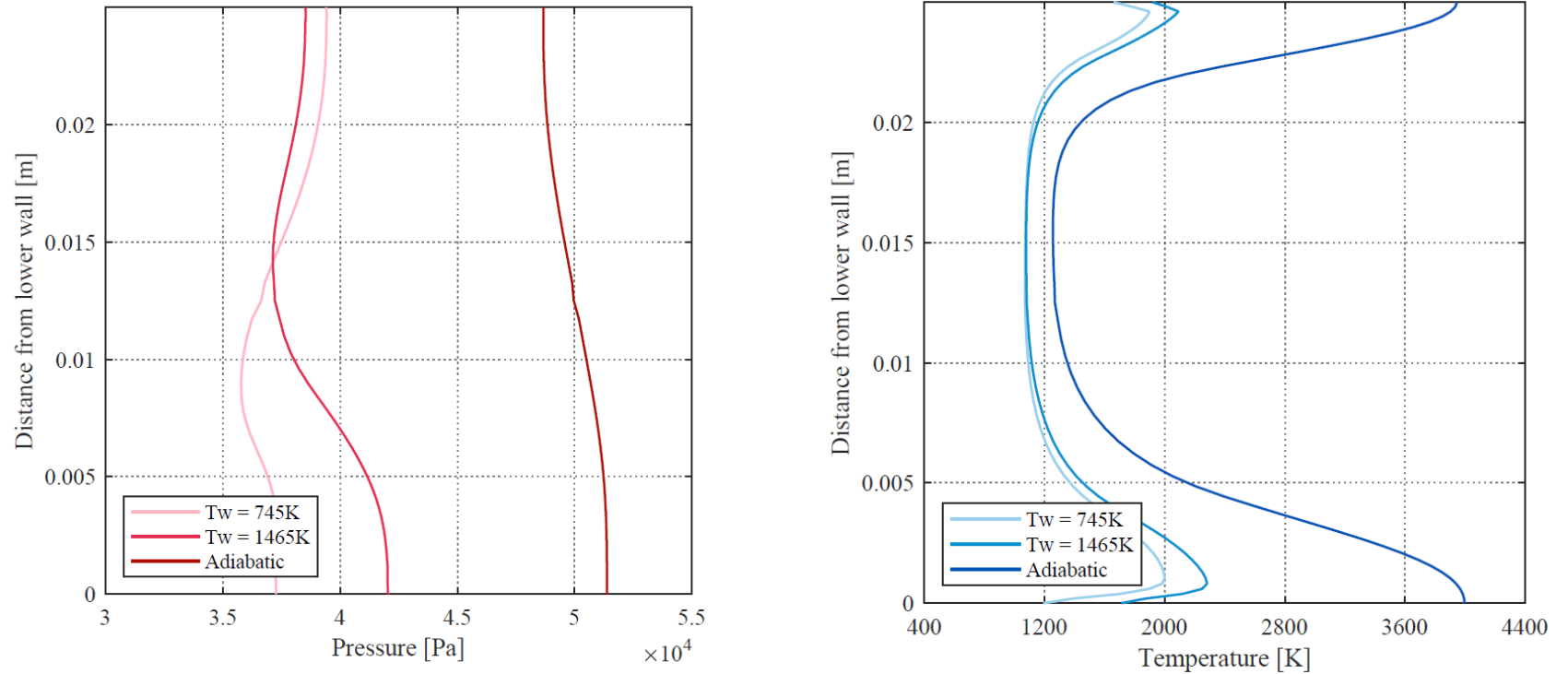


Fig. 12: Pressure and temperature profiles at the isolator exit for different wall boundary conditions.

Case	π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
$T_w = 1465K$	0.0793	0.9442	0.7898	0.7921
$T_w = 745K$	0.0908	0.9495	0.7956	0.8127
Adiabatic	0.0332	0.9035	0.7661	0.6925

Table 3: Performance parameters for different wall boundary conditions.

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Two-Dimensional Geometry: Chemical and Thermal Non-Equilibrium

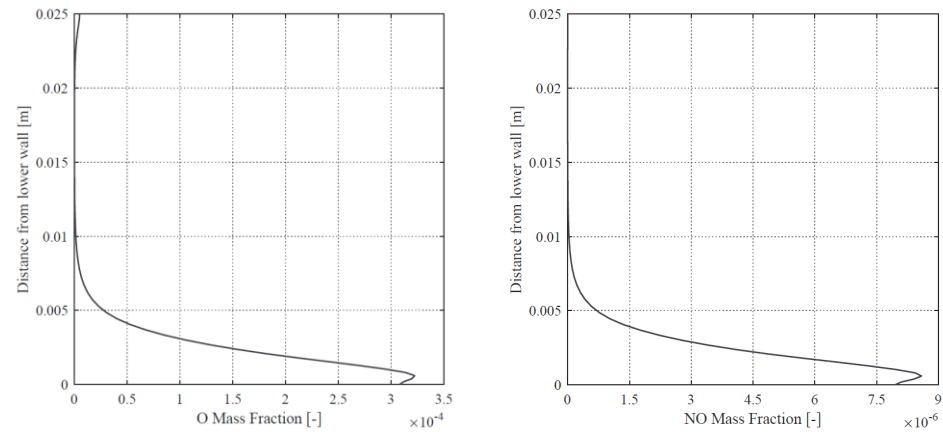


Fig. 14: O and NO mass fractions at the isolator exit for the chemically reacting flow solution.

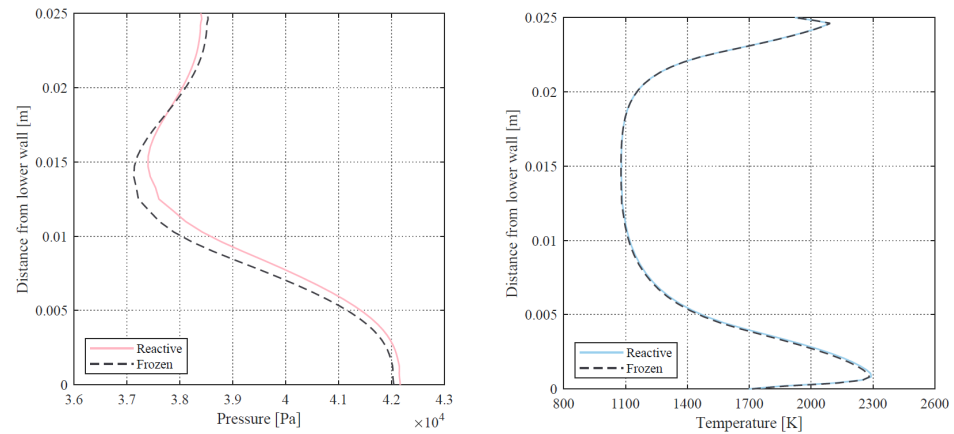


Fig. 15: Pressure and temperature profiles at the isolator exit for the chemically reacting flow solution.

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Two-Dimensional Geometry: Chemical and Thermal Non-Equilibrium

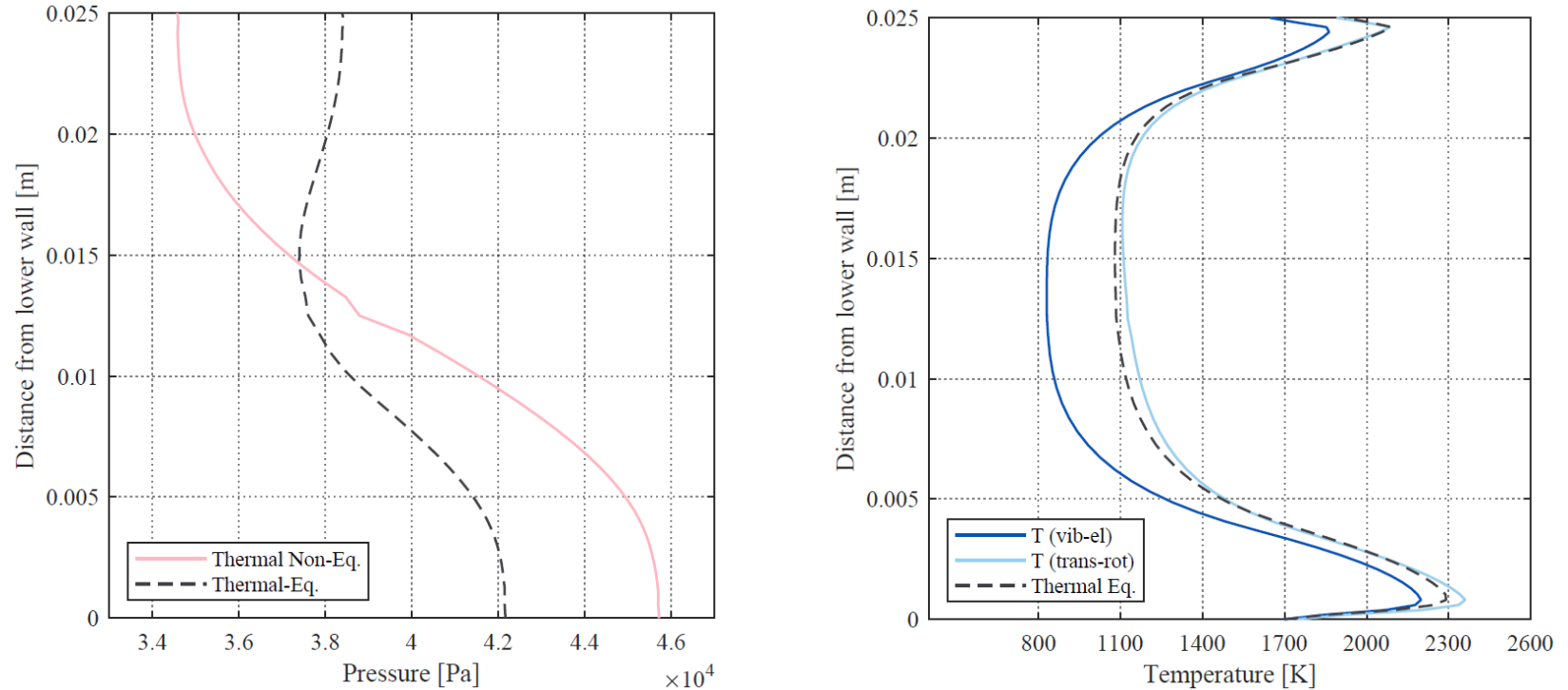


Fig. 16: Pressure and temperature profiles at the isolator exit for the thermal non-equilibrium flow solution.

Case		π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
Thermal Equilibrium	Frozen	0.0793	0.9442	0.7898	0.7921
	Reactive	0.0781	0.9440	0.7897	0.7916
Thermal Non-equilibrium		0.0652	0.9596	0.8183	0.7858

Expectedely, similar exit profiles lead to similar performance parameters.

Table 4: Performance parameters for thermal equilibrium and non-equilibrium solutions.

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Axisymmetric Flow

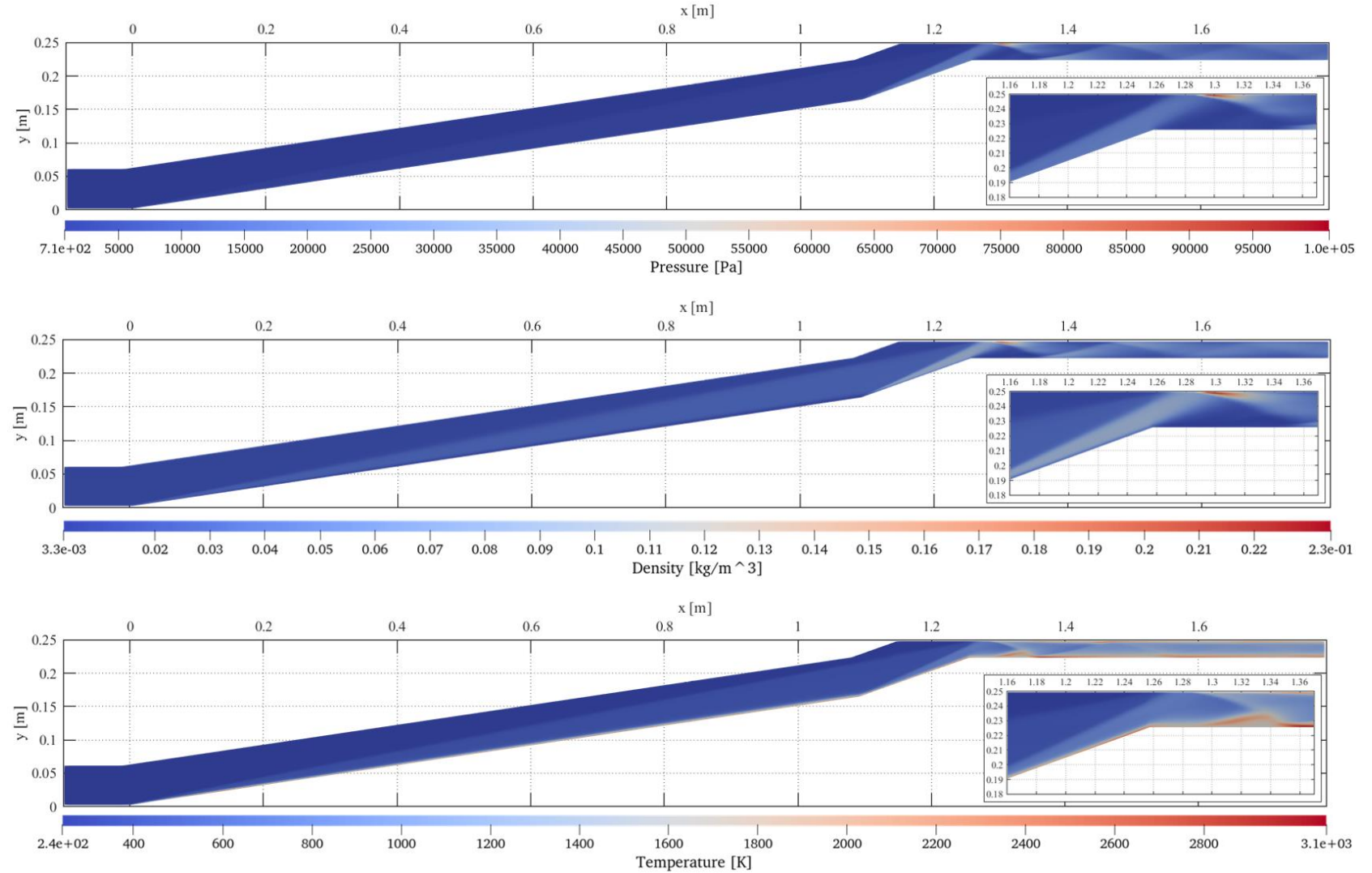


Fig. 17: Pressure, temperature and density fields obtained for the frozen-flow solution of the two-dimensional geometry.

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Axisymmetric Flow

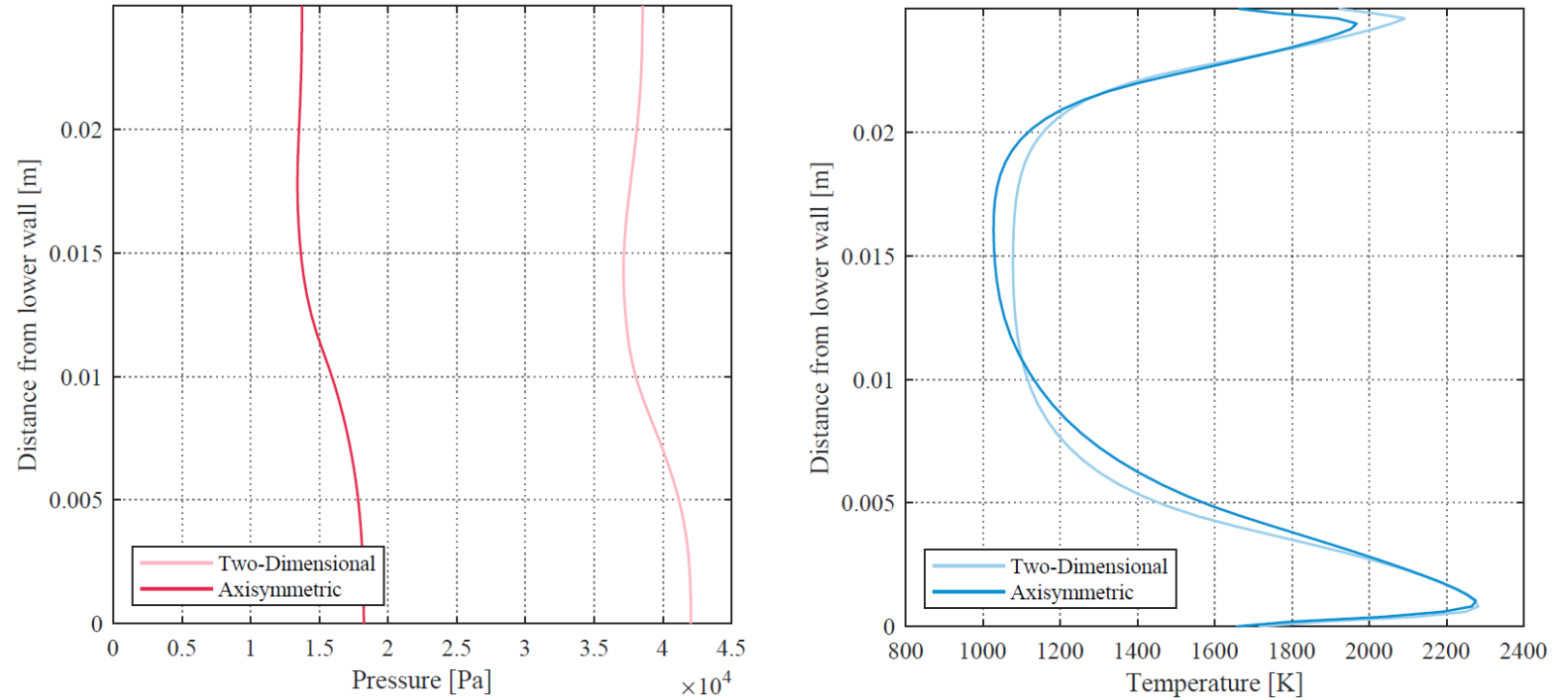


Fig. 18: Pressure and temperature profiles at the isolator exit, for the axisymmetric and two-dimensional configurations.

Case		π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
Thermal Equilibrium	Frozen	0.0327	0.9181	0.6833	0.6276
	Reactive	0.0305	0.9172	0.6803	0.6068
Thermal Non-equilibrium		0.0243	0.9492	0.7274	0.5906

Table 5: Performance parameters for thermal equilibrium and non-equilibrium solutions.

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Axisymmetric Flow

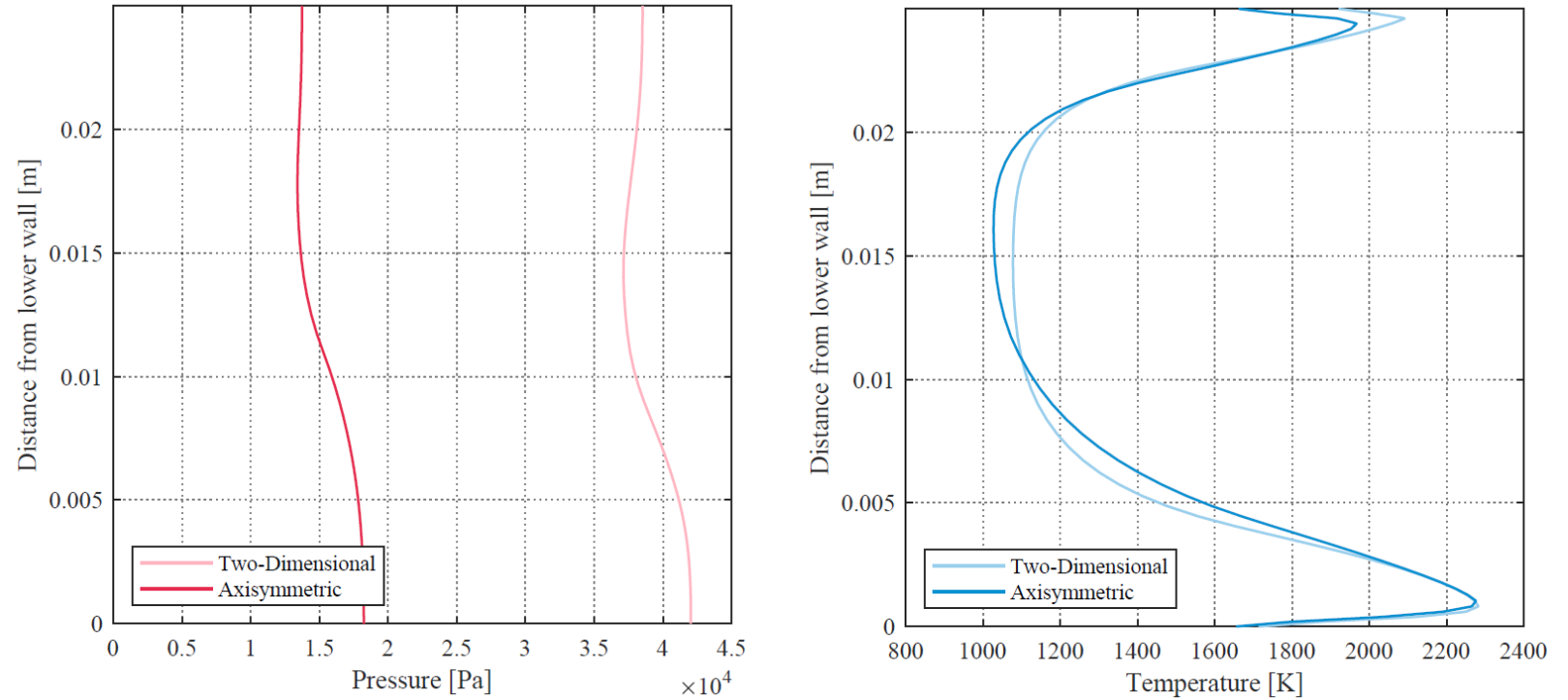


Fig. 19: Pressure and temperature profiles at the isolator exit, for the axisymmetric and two-dimensional configurations.

Case		π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
Thermal Equilibrium	Frozen	0.0327	0.9181	0.6833	0.6276
	Reactive	0.0305	0.9172	0.6803	0.6068
Thermal Non-equilibrium		0.0243	0.9492	0.7274	0.5906

Table 5: Performance parameters for thermal equilibrium and non-equilibrium solutions.

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Geometry Parametric Study: Increased Number of Ramps (2D)

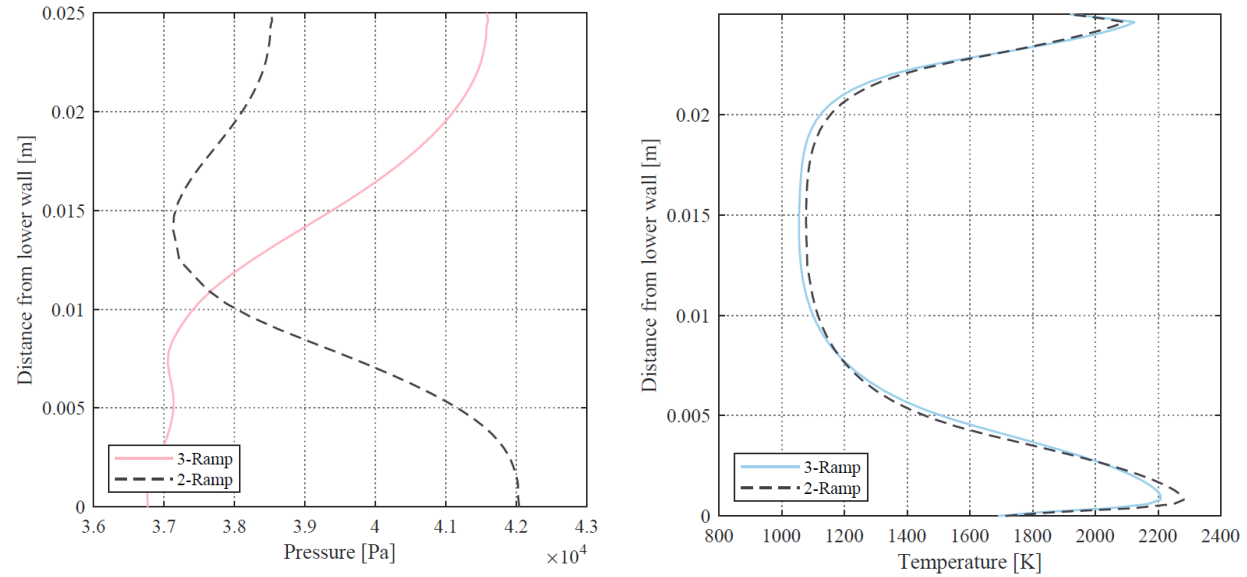
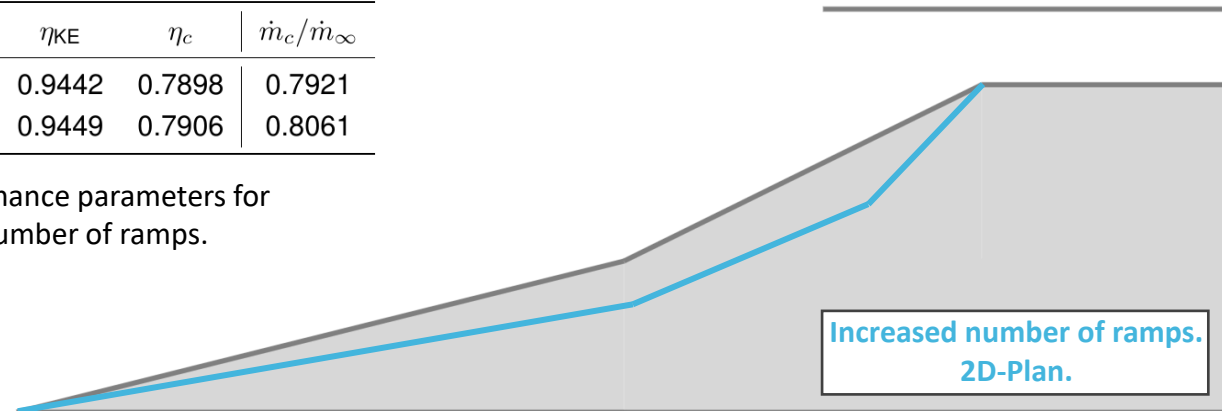


Fig. 20: Pressure and temperature profiles at the isolator exit, for different number of ramps.

Case	π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
Two Ramp	0.0793	0.9442	0.7898	0.7921
Three Ramp	0.0813	0.9449	0.7906	0.8061

Table 6: Performance parameters for different number of ramps.



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Geometry Parametric Study: Increased Compression Ratio (2D)

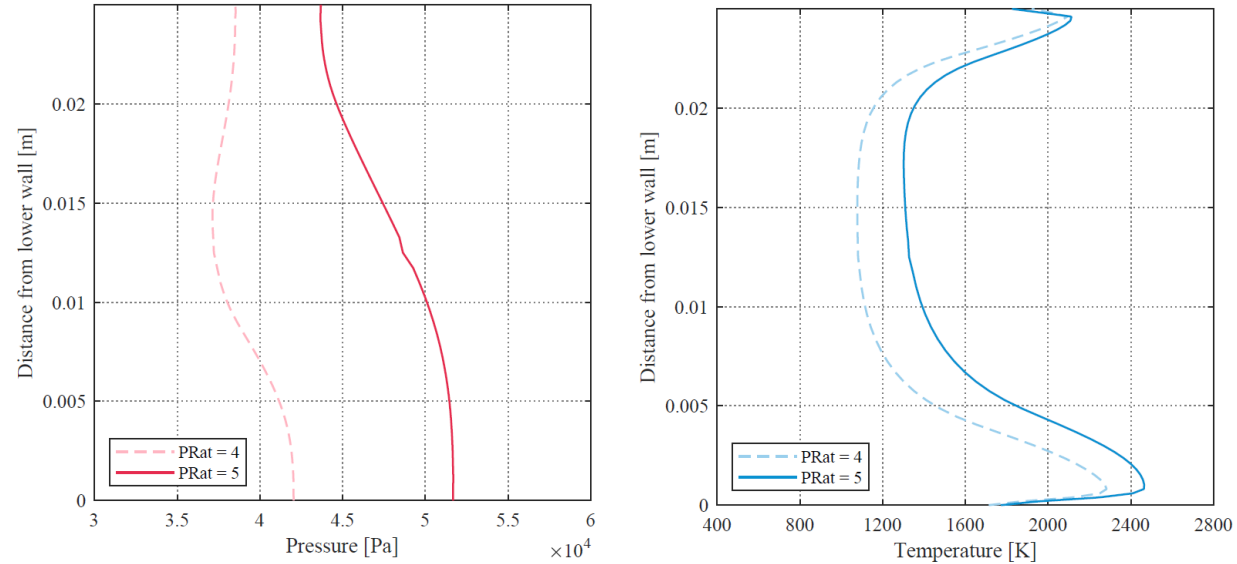
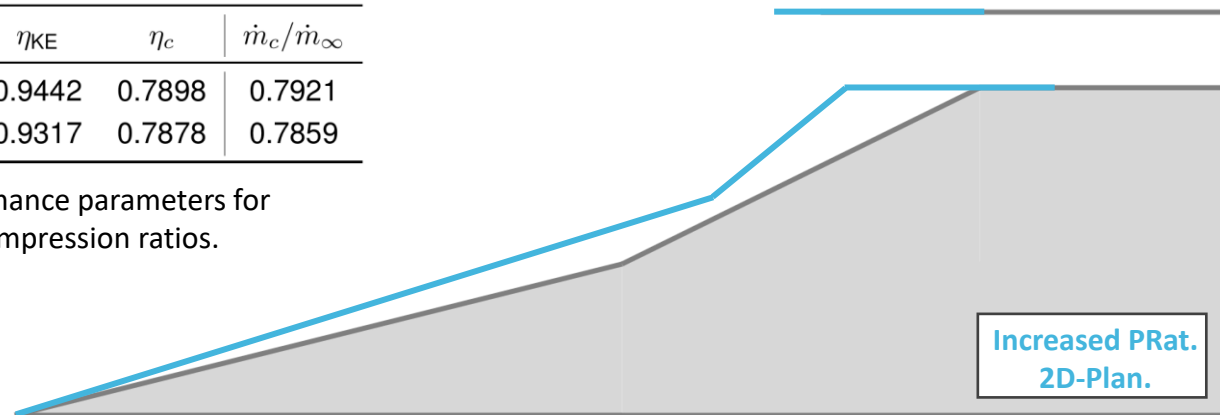


Fig. 21: Pressure and temperature profiles at the isolator exit, for different compression ratios.

Case	π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
PRat = 4	0.0793	0.9442	0.7898	0.7921
PRat = 5	0.0489	0.9317	0.7878	0.7859

Table 7: Performance parameters for different compression ratios.



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Geometry Parametric Study: Increased Compression Ratio (2D)

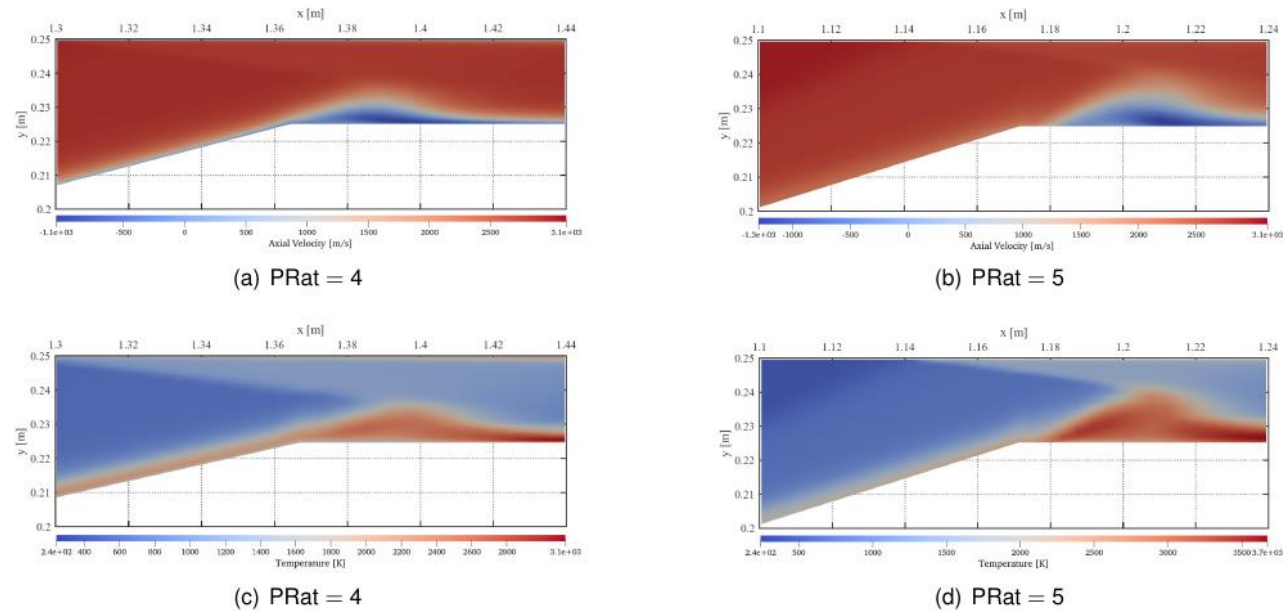
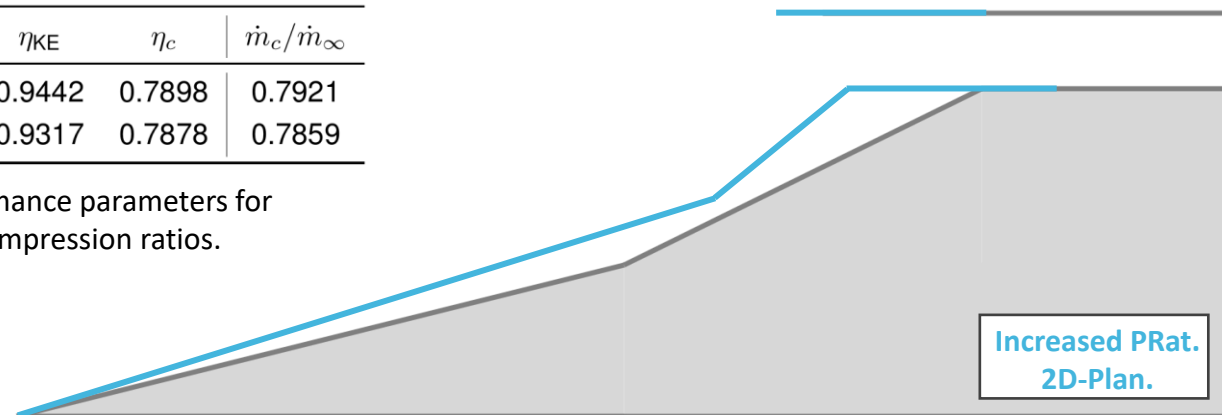


Fig. 22: Velocity (top) and temperature (bottom) profiles for different compression ratios.

Case	π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
PRat = 4	0.0793	0.9442	0.7898	0.7921
PRat = 5	0.0489	0.9317	0.7878	0.7859

Table 7: Performance parameters for different compression ratios.



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Geometry Parametric Study: Variation of the Isolator Length (2D)

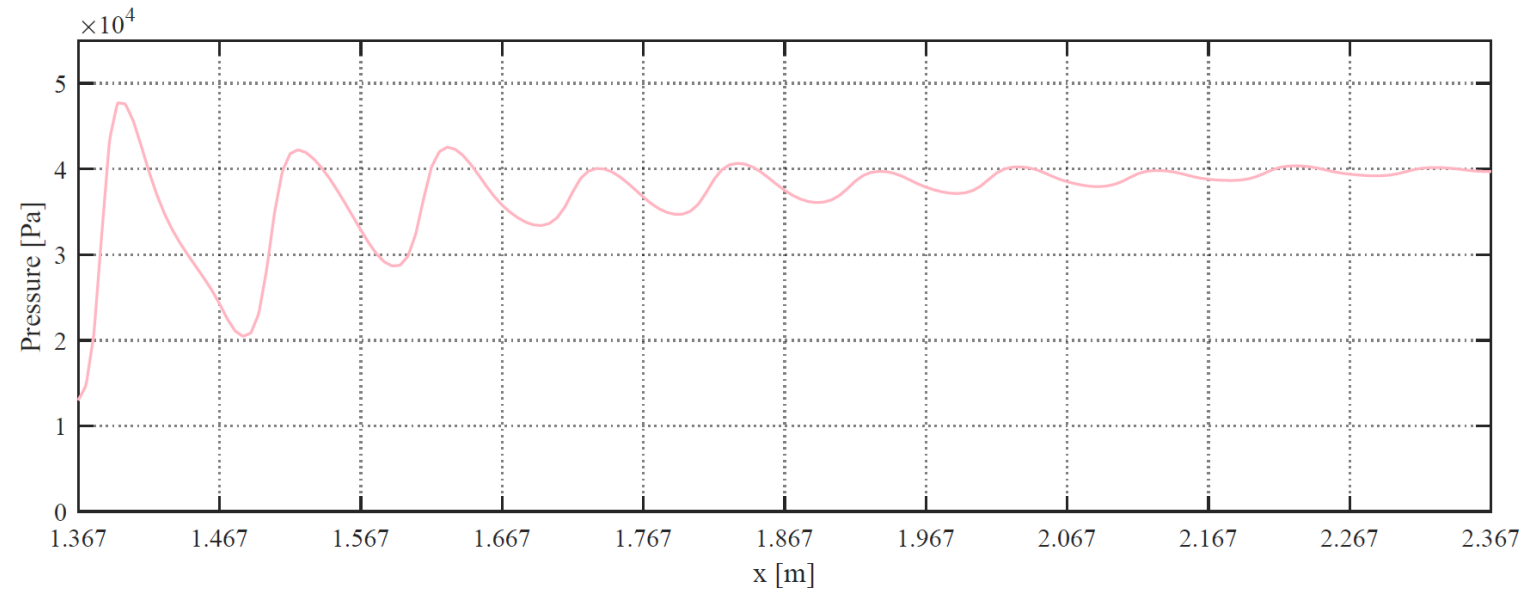
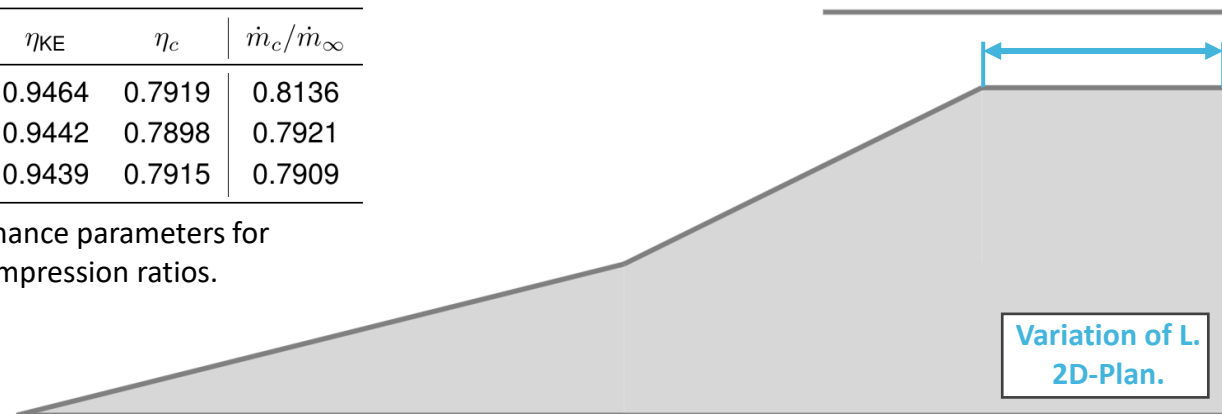


Fig. 23: Pressure along the isolator centreline, for an isolator length of 1m.

Case	π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
L = 0.15m	0.0983	0.9464	0.7919	0.8136
L = 0.5m	0.0793	0.9442	0.7898	0.7921
L = 1m	0.0697	0.9439	0.7915	0.7909

Table 8: Performance parameters for different compression ratios.



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Geometry Parametric Study: Variation of the Isolator Length (2D)

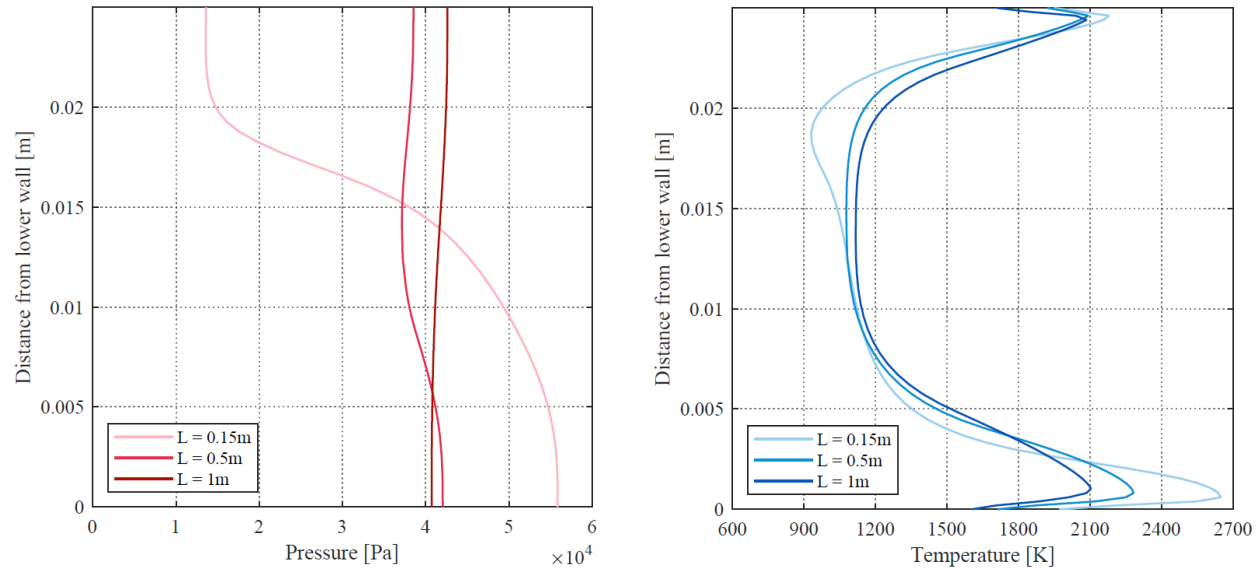
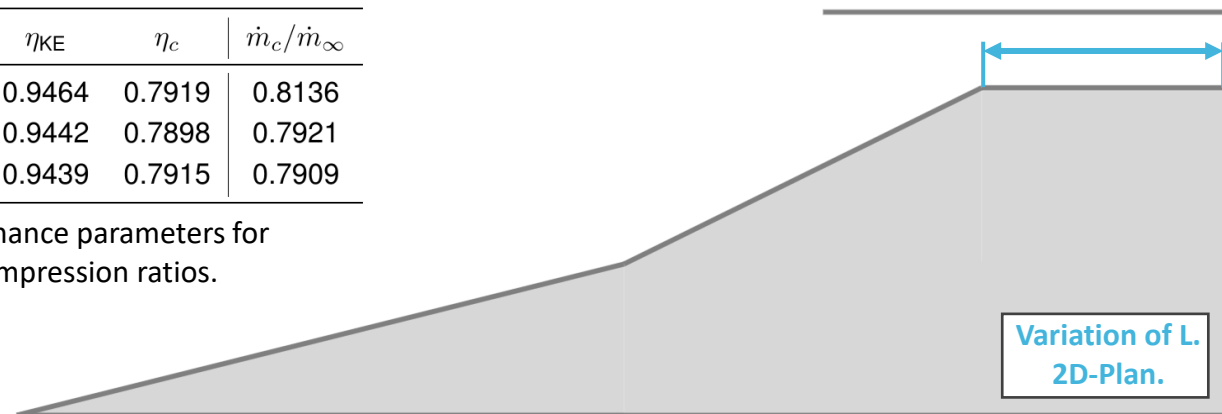


Fig. 24: Pressure and temperature profiles at the isolator exit, for different isolator lengths.

Case	π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
L = 0.15m	0.0983	0.9464	0.7919	0.8136
L = 0.5m	0.0793	0.9442	0.7898	0.7921
L = 1m	0.0697	0.9439	0.7915	0.7909

Table 8: Performance parameters for different compression ratios.



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Geometry Parametric Study: Increased Contraction Ratio (2D)

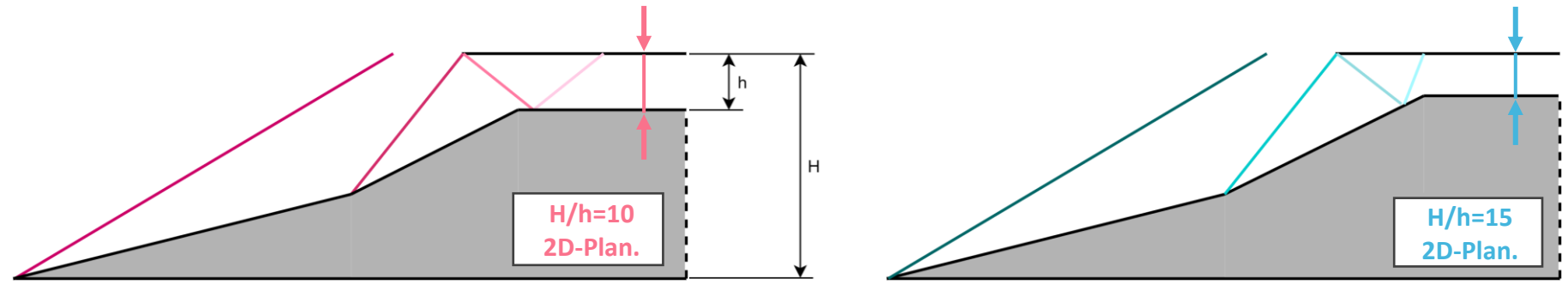


Fig. 25: Shock wave structure for a contraction ratio of 10 (left) and 15 (right).

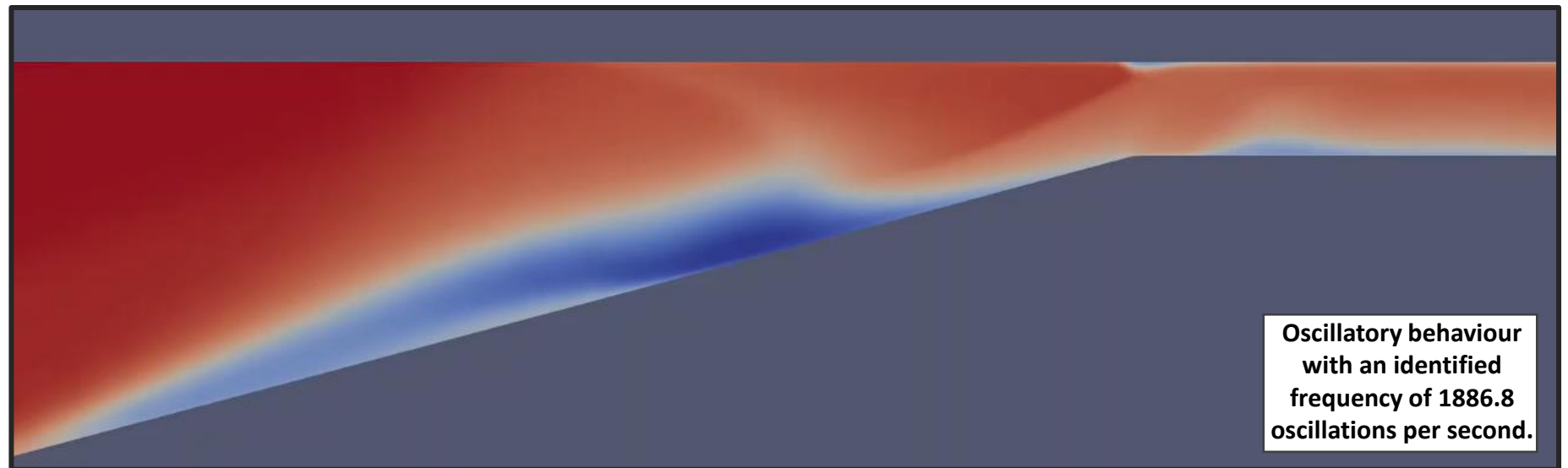


Fig. 26: Observed instability for the case with a contraction ratio of 15.

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Geometry Parametric Study: Variation of the Expansion Corner Shape (2D)

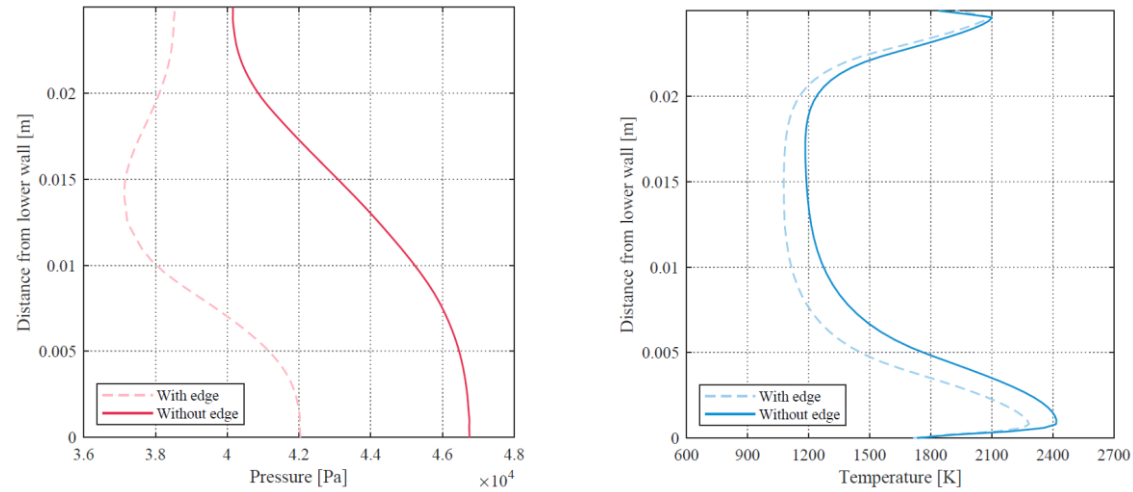


Fig. 27: Pressure and temperature profiles at the isolator exit, for different expansion corner shapes.

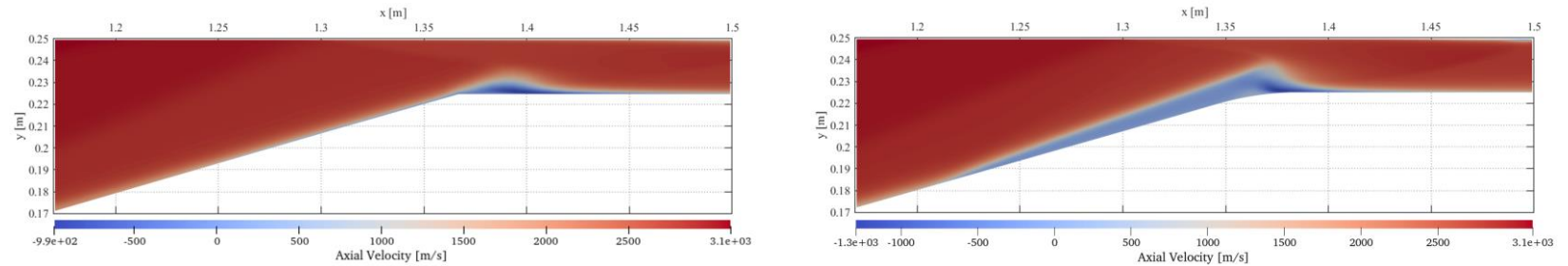


Fig. 28: Separation bubble for different expansion corner shapes.

Case	π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
With edge	0.0793	0.9442	0.7898	0.7921
Without edge	0.0598	0.9362	0.7869	0.7838

Table 9: Performance parameters for different expansion corner shapes.

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Geometry Parametric Study: Axisymmetric Configuration

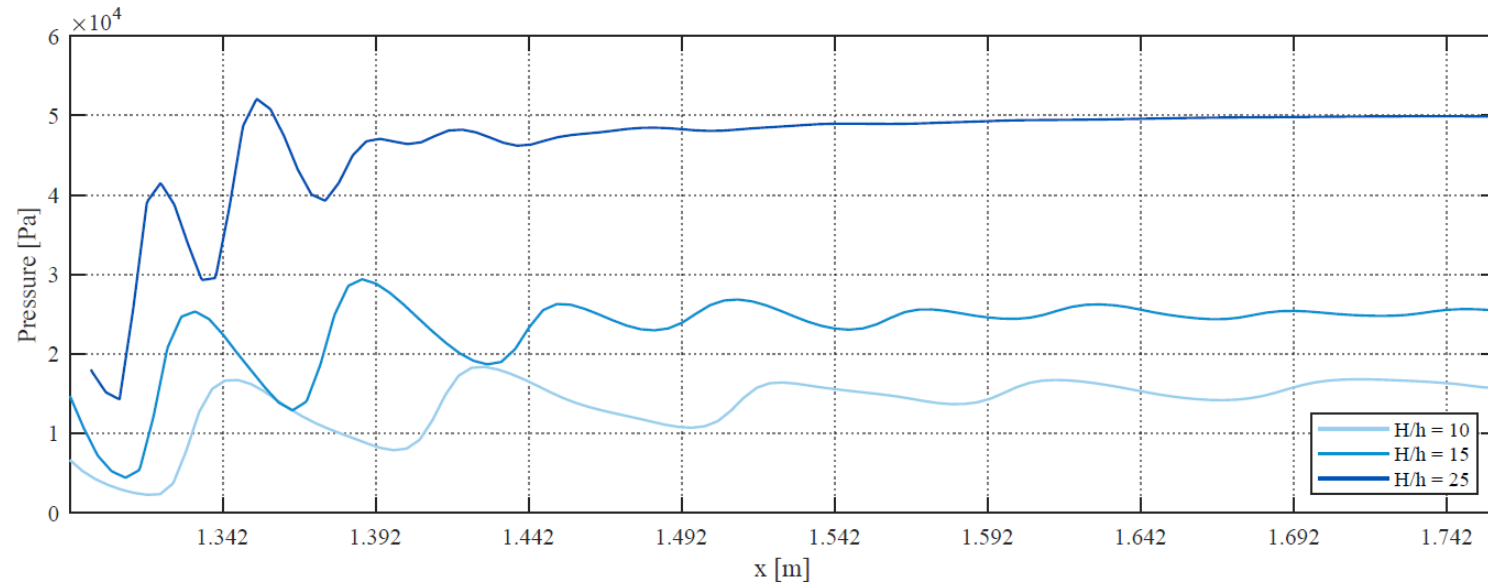


Fig. 29: Pressure along the isolator centreline, for different contraction ratios.

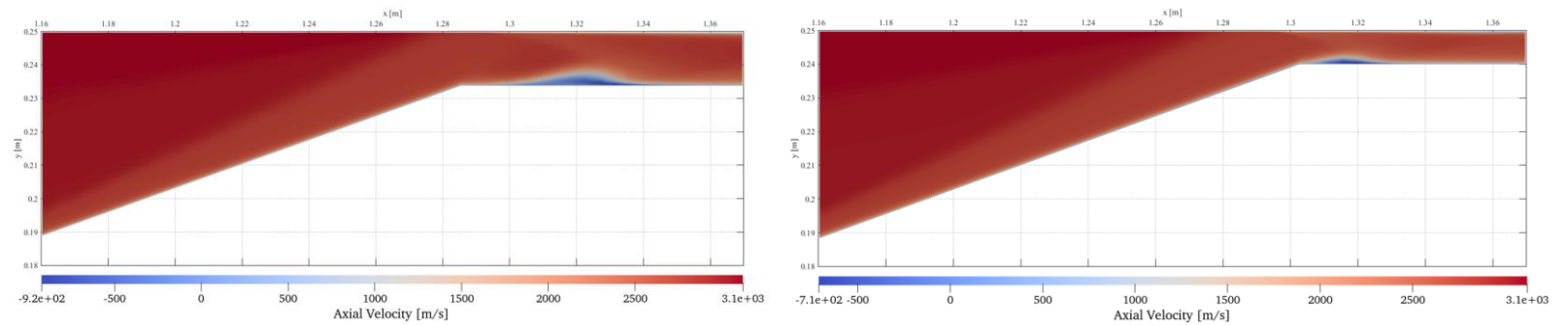


Figure 30: Separation bubbles for different contraction ratios.

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Geometry Parametric Study: Axisymmetric Configuration

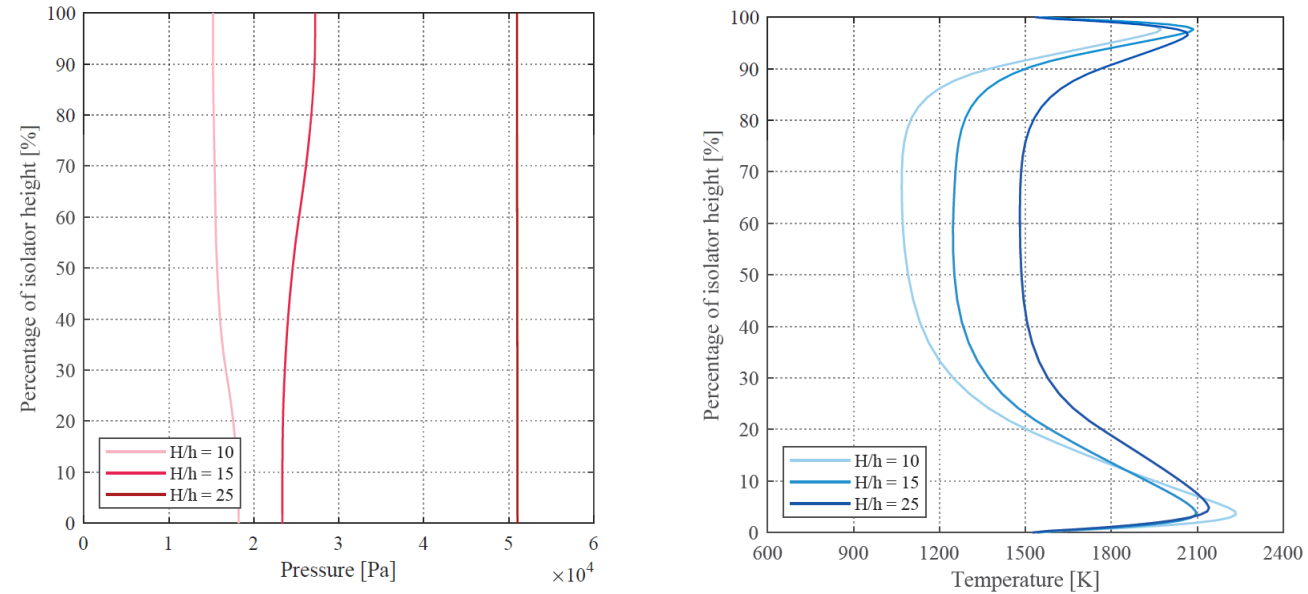
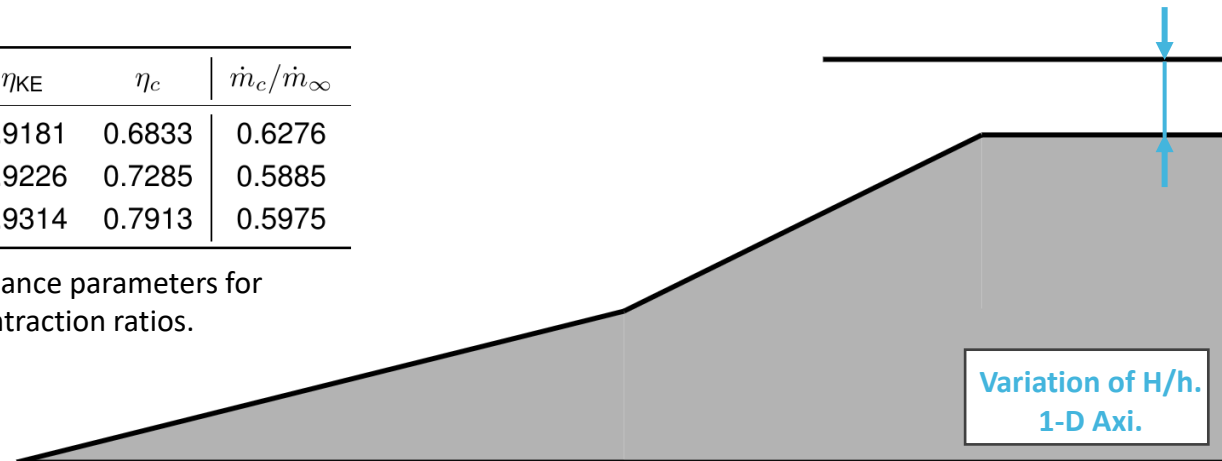


Fig. 31: Pressure along the isolator centreline, for different contraction ratios.

Case	π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
H/h = 10	0.0327	0.9181	0.6833	0.6276
H/h = 15	0.0350	0.9226	0.7285	0.5885
H/h = 25	0.0382	0.9314	0.7913	0.5975

Table 10: Performance parameters for different contraction ratios.



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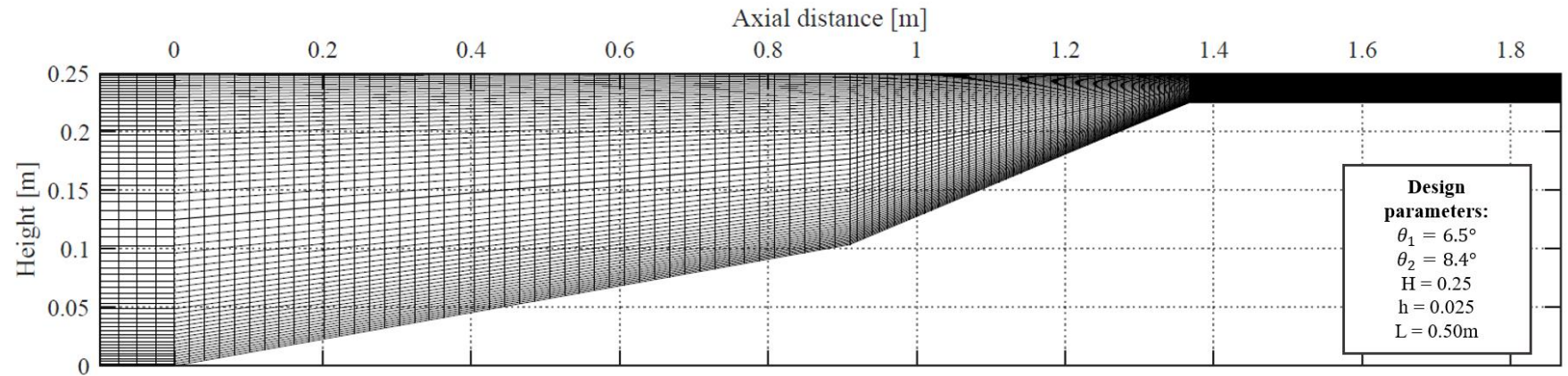


Fig. 32: Adapted grid used in the study of operation at off-design conditions.

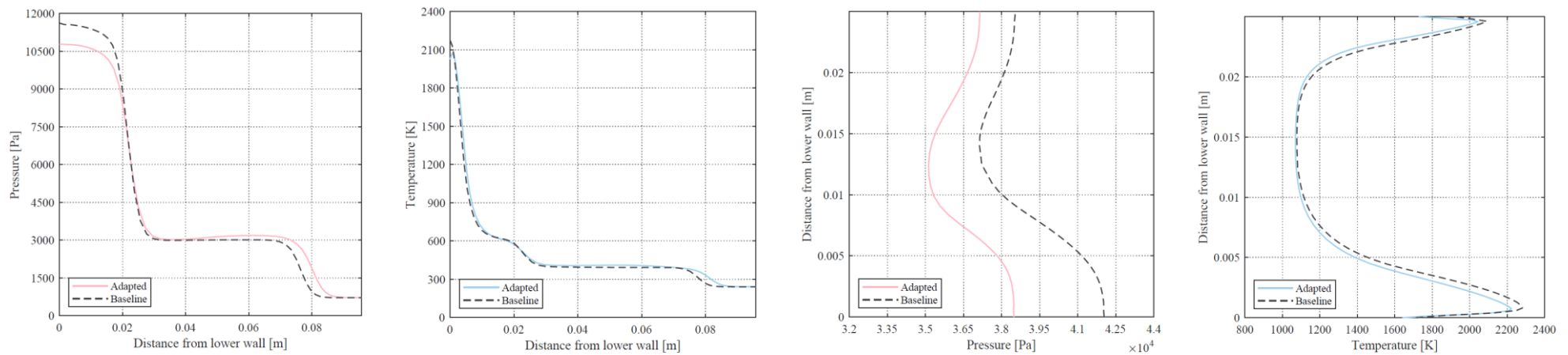


Fig. 33: Comparison of the baseline and adapted grids at a freestream Mach number of 10.

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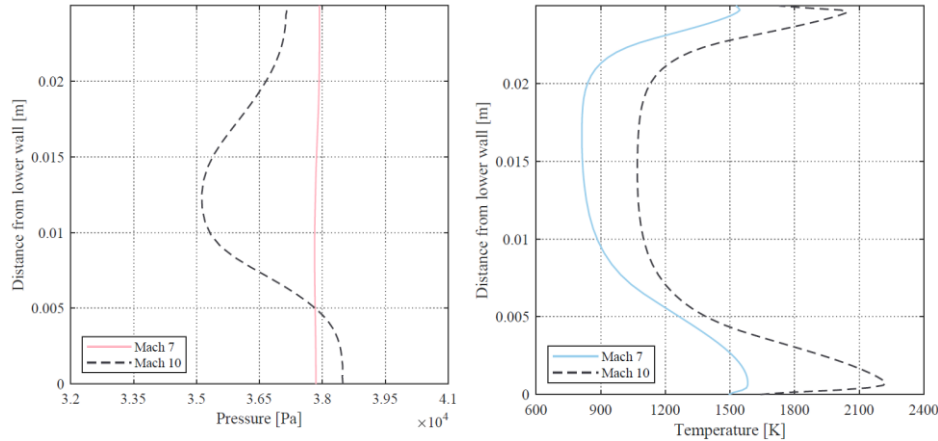


Fig. 34: Pressure and temperature profiles at the isolator exit, for different trajectory points (2D).

Case	π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
Mach 10	0.0833	0.9458	0.7880	0.7718
Mach 7	0.0896	0.8920	0.7370	0.4381

Table 11: Performance parameters for different trajectory points (2D).

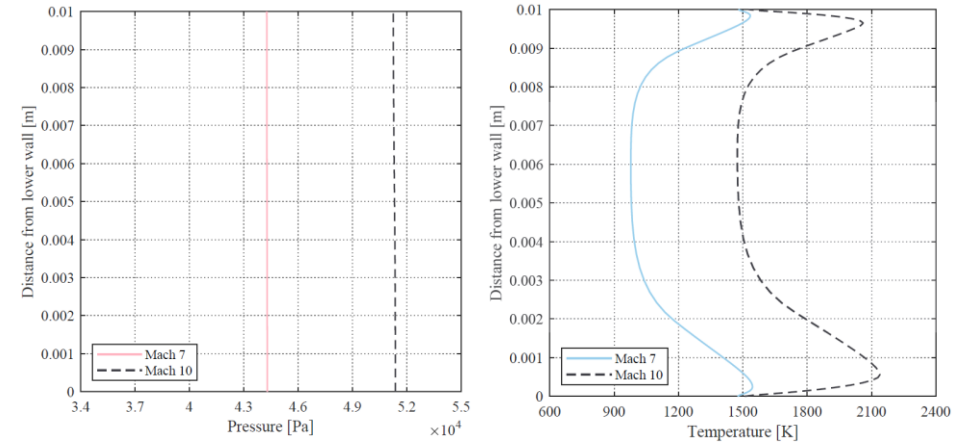


Fig. 35: Pressure and temperature profiles at the isolator exit, for different trajectory points (axisymmetric).

Case	π_c	η_{KE}	η_c	\dot{m}_c/\dot{m}_∞
Mach 10	0.0358	0.9316	0.7920	0.5922
Mach 7	0.0884	0.8914	0.7350	0.3355

Table 12: Performance parameters for different trajectory points (axisymmetric).

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- Reproduction of a case study from the literature for a trajectory point of Mach 10, with **minor discrepancies found** in terms of peak pressure and isolator exit pressure;
- Lower wall temperatures were shown to improve performance, while an adiabatic wall results in unrealistically high wall temperatures.
- Chemical dissociation was found to be negligible while thermal non-equilibrium was found to occur and impact performance.
- An axisymmetric configuration was compared against a two-dimensional one, and was found to under-perform for all considered cases;
- The variation of some geometric parameters were shown to impact performance, with one geometric change leading to inlet unstart;
- Both the two-dimensional and axisymmetric configurations were **able to operate at an off-design trajectory point** of Mach 7.



Fig. 36: Burrows Kurkov [7] frozen flow simulation already implemented in SPARK.



Fig. 37: Attempt to reproduce the supersonic combustions experiments conducted in the DLR facilities in SPARK.

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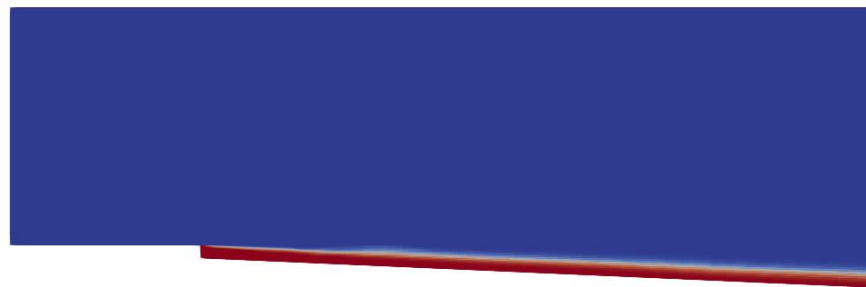


Fig. 36: Burrows Kurkov [7] frozen flow simulation already implemented in SPARK.

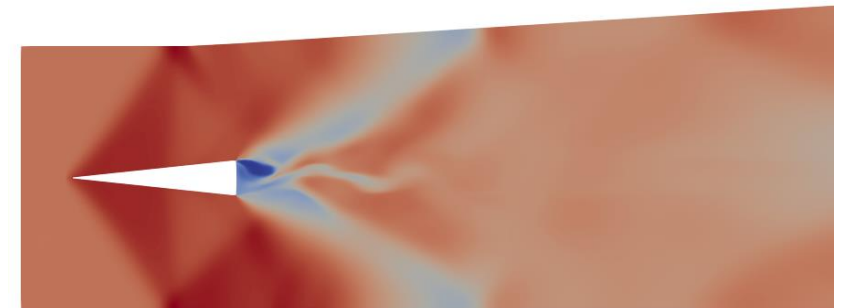


Fig. 37: Attempt to reproduce the supersonic combustions experiments conducted in the DLR facilities [8] in SPARK.

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